

ON THE INFLUENCE OF MICROSTRUCTURE UPON CRACK PROPAGATION MECHANISM AND FRACTURE TOUGHNESS

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Using a combination of numerical and experimental methods two different types of low strength steels Fe 510 have been investigated for describing the influence of microstructure on crack propagation mechanism and fracture toughness. The microstructure parameters have been determined by means of quantitative metallographic techniques.

INTRODUCTION

Today one of the most important aims in technical research on structural materials is to investigate the influence of microstructure on crack propagation mechanism and fracture toughness. During plastic deformation in ductile metals, damage is mainly described by nucleation (a), growth (b) and coalescence (c) of voids (1,2,3). For ductile fracture the latter stages, void growth and coalescence, are more important. McClintock (4,5) and Rice and Tracey (6) have shown that void growth strongly depends upon the rate of specimen extension and the state of stress, especially upon the ratio of mean stress to effective flow stress. The coalescence of the first voids ahead of the crack tip can be defined as the onset of stable crack growth, indicated by  $J_1$  or  $\delta_1$ , respectively.

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Definition of stress and strain state parameters

Three parameters of stress and strain state are used throughout; effective flow stress  $\sigma_v$ , mean stress  $\sigma_m$  and effective plastic strain  $\epsilon_v^p$ , defined as follows in terms of the principal stresses  $\sigma_1, \sigma_2$  and  $\sigma_3$ , and the increments of principal plastic strains  $d\epsilon_1^p, d\epsilon_2^p$  and  $d\epsilon_3^p$ .

$$\sigma_v = \sqrt{\frac{1}{2} [(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2]} \quad (1)$$

$$\sigma_m = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3} \quad (2)$$

$$d\epsilon_v^p = \sqrt{\frac{2}{3} [(d\epsilon_1^p)^2 + (d\epsilon_2^p)^2 + (d\epsilon_3^p)^2]} \quad (3)$$

The two stress parameters can be combined into a single non-dimensional parameter  $\sigma_m/\sigma_v$  which characterizes a stress state and is a measure of its "triaxiality". In a uniaxial tension test  $\sigma_m/\sigma_v$  is 0.3, before necking. According to Bridgman (7),  $\sigma_m/\sigma_v$  and  $\epsilon_v^p$  in the central region of the specimen, where failure initiates, can be described as:

$$\frac{\sigma_m}{\sigma_v} = \frac{1}{3} + \ln\left(\frac{d}{4\rho} + 1\right) \quad (4)$$

$$\epsilon_v^p = 2 \cdot \ln\left(\frac{d_0}{d}\right) \quad (5)$$

where  $d_0$  = original specimen diameter  
 $d$  = actual specimen diameter  
 $\rho$  = actual notch radius

The same non-dimensional stress state parameter ( $\sigma_m/\sigma_v$ ) has been used by several authors (8,9,10) to present ductile failure loci in which the strain to initiate failure is presented as a function of the state of stress ( $\sigma_m/\sigma_v$ ). In this work the influence of stress state upon the plastic strain at failure is evaluated on axisymmetric, circumferentially notched tensile specimens for six different notch radii  $\rho_0$  ( $\rho_0 = 0.25; 0.5; 1; 2; 4$  mm and  $\rho_0 = \infty$ ).

Finite element (FE) analysis (11,12) have shown that both the effective plastic strain and the severity of the stress state in the centre of the specimen cannot be estimated precisely by Bridgman's formula in the case of sharp notches. When the notch

radius becomes larger the agreement between both values becomes better. Within the scope of this work, these critical strain and stress values according to Bridgman will be compared with the results of FE-calculations.

The calculations have been carried out on specimens with sharp notches ( $\rho_0 = 1 \text{ mm}$  and  $0.25 \text{ mm}$ ) with the eight-node element mesh (figure 1); a reduced integration scheme (2x2) has been adopted in order to avoid the violation of incompressibility conditions. The deformation of the mesh geometry has been taken into account using the so called "updated lagrange" to modify the coordinates for each load step. One fourth of the specimen was sufficient to idealize the FE-model (see also figure 1).

## RESULTS

### Experimental results

The tensile and fracture tests have been performed on two types of steel Fe 510, one of them with a reduced carbon content and higher purity; in comparison to the standard version (0.0195%) the sulphur content of the pearlite reduced quality was determined to 0.002%. Finally, to assure a similar strength level, it contained some Vanadium and Niobium. For either steels, the microstructure is characterized by ferrite with bands of pearlite, being less pronounced in the pearlite reduced quality. Due to the addition of the microalloying elements, the mean ferrite grain size for the pearlite-reduced steel is smaller than for the other material, the values being  $5.5 \mu\text{m}$  and  $15.0 \mu\text{m}$  (13).

Based on the lower sulphur content, the mean distance of MnS-inclusions  $S$  has been determined to  $110.3 \mu\text{m}$  in case of pearlite-reduced quality, in contrast to  $42.2 \mu\text{m}$  for the standard version. These values and the results of the tensile tests on notched and unnotched specimens are listed in table 1.

### Numerical results

The results of the tensile tests are presented in figure 2a (Fe 510) und 2b (pearlite-reduced). In the figure above the load is plotted as a function of the reduction of the specimen diameter for  $\rho_0 = 0.25 \text{ mm}$ , below for  $1 \text{ mm}$ . The dashed lines result from experiment, the solid ones are calculated. The comparison reveals a quite good agreement, but as soon as ductile damage starts, the difference between the curves increases. The main problem is to detect the point of failure initiation; FE-calculations do not indicate this phenomenon, e.g. after some work hardening a sharp drop of load, suggesting a sudden reduction in cross section area. Nevertheless, the results of this work suggest that initiation might correspond to a first deviation between experiment and calculated curve, beyond maximum load. In figure 2 these points are marked with arrows and indices  $i$ .

Figures 3a and 3b show the effective plastic strain  $\epsilon_V^p$  as a function of the distance from the specimen centre, with the applied load as parameter. The values of  $\epsilon_V^p$  increase from the centre of

the specimen up to the notch with the maximum value at the notch root. The corresponding values according to Bridgman (eq. (5)) are constant (dashed lines).

Corresponding to figure 3, figures 4a and 4b show the stress state parameter. The  $\epsilon_V^p$ - and the  $\sigma_m/\sigma_V$ -values for initiation of fracture are again marked with arrows. It can be seen, that, for  $\rho_0 = 0.25$  mm, the maximum values were found near the notch root, for  $\rho_0 = 1$  mm, these maximum values disappear more and more with increasing plasticity. As simple failure initiation condition it can be assumed, that  $\epsilon_V^p$  must reach a critical value at the root of the notch; as figures 3 and 4 indicate, the corresponding value for the stress state ( $\sigma_m/\sigma_V$ ) shows a minimum. On the other hand - from a microscopic and physical point of view -, failure can not depend upon the stress and strain at a certain point, but over a characteristic length or volume, related to the microstructure. Thus, a modified failure initiation condition is necessary;  $\epsilon_V^p$  must exceed a critical value over a certain critical distance  $l_C$ , and this distance  $l_C$ , known as the material size parameter, is not necessarily located immediately ahead of the notch but may be found in the centre of the sample. So, for predicting failure initiation, both the  $\sigma_m/\sigma_V$ - and  $\epsilon_V^p$ -values have to be taken into account.

In this work the microstructural critical distance  $l_C$  has been determined by light microscope. Figure 5 shows the photo of two notched specimens with  $\rho_0 = 0.25$  mm (above) and  $\rho_0 = 1$  mm (below). The tensile tests had been stopped immediately beyond maximum load and the specimens afterwards have been examined metallographically; therefore they had been cut in the centre in axial direction. One can see very well, that for  $\rho_0 = 0.25$  mm failure initiates near the tip of the notch, while, if  $\rho_0$  is large enough initiation begins in the centre of the specimen. The critical distance  $l_C$  was determined to 0.52 mm (see also figure 5). The values for  $l_C$ ,  $\sigma_m/\sigma_V$  and  $\epsilon_V^p$ , corresponding to initiation, are listed in table 1.

Figure 6 shows the effective plastic strain as a function of stress state. Obviously there is a strong dependency for both steels. The hollow symbols result from Bridgman's equations (eqs. (4) and (5)). Both FE-calculation and Bridgman's formula show a strong decrease of the effective plastic strain with increasing triaxiality, until, at about  $\sigma_m/\sigma_V \sim 1$ , the curves approach a rather constant level of about  $\epsilon_i^m = 0.14$  and 0.58, respectively. As it can be seen from the diagram, two geometries have been compared; while, according to Bridgman, the smaller notch radii show the higher values  $\sigma_m/\sigma_V$ , the FE calculations seem to indicate the opposite. All these curves can be approached very well by an exponential function, viz:

$$\epsilon_f^* = \alpha \cdot \exp(-\beta \cdot \sigma_m/\sigma_V) + \epsilon_i \quad (6)$$

The values for  $\beta$  were found between 5 and 16, that means considerably above the theoretical value 1.5 (8).

Correlation between microstructure and fracture toughness

The fracture mechanics values have been determined according to ASTM E813 (14) on CT specimens with  $a/W = 0.6$  and 20% side grooves. At the onset of crack extension the  $J_i$ -values have been evaluated using the direct current potential drop (DCPD)-method. Figure 7 shows the R-curves for the steels examined, resulting from fracture mechanics tests. Due to the reduced carbon content and to microalloying, the pearlite-reduced quality shows by far the better crack extension behaviour. The  $J_i$ -values are marked by arrows.

In order to describe the relationship between microstructure and ductile fracture, the critical strain criterion was applied inside this work. There are different models to describe the strain distribution at the crack tip, e.g. McMeeking (15), Rice and Johnson (16) and the HRR-field (17). In (10) the strain distribution for each of these models has been discussed and compared quantitatively. To determine the effective plastic strain, the HRR-solution was used:

$$\epsilon_v^p = \alpha \cdot \epsilon_y \cdot \left( \frac{J}{\alpha \cdot \sigma_y \cdot \epsilon_y \cdot I_N \cdot r} \right)^{N/(N+1)} \cdot \hat{\epsilon}^p(\theta, N) \quad (7)$$

with

- $\alpha, N$  = Ramberg-Osgood constants
- $\sigma_y$  = yield stress
- $\epsilon_y$  =  $\sigma_y/E$  is the yield strain
- $E$  = Young's modulus
- $I_N, \theta$  = dimensionless constants, HRR-field function
- $\hat{\epsilon}^p(\theta, N) = [\hat{\epsilon}_e(\theta, N)]^N$

and for initiation

$$\begin{aligned} J &= J_i & \epsilon_v^p &= \epsilon_i \\ r &= l_c \end{aligned}$$

In table 1 the calculated values for  $l_c$  are listed, being about three times the magnitude of the mean distance of MnS-inclusions. In any case, they are considerably smaller than those determined by light microscope.

SUMMARY

Two types of steel Fe 510 have been investigated in order to find a correlation between microstructure and fracture toughness. Up to the onset of instability the global material behaviour can be described very well by finite element analyses using the so called "updated lagrange". It could also be shown that the Bridgman formula cannot describe

the strain and stress distribution corresponding to initiation, if the notch radii of the specimen are small.

When trying to correlate between microstructure and fracture toughness, the following requirements must be fulfilled:

- a proper criterion for ductile fracture must be chosen
- stress or strain distribution ahead of the crack tip must be known
- a good conception for determining the microstructural critical distance  $l$  is necessary. Inside this work, the values for  $l$  proved to be about three times the mean distance of MnS-inclusions. The values observed by light microscope proved to be higher.

#### ACKNOWLEDGEMENT

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steel	experiment $\sigma_m/\sigma_y$   $\epsilon_p/\epsilon_y$	FE-calculation $\sigma_m/\sigma_y$   $\epsilon_p/\epsilon_y$	N	$\sigma_y$ [MPa]	S [ $\mu\text{m}$ ]	cal. $l_c$ [ $\mu\text{m}$ ]
Fe 510	$\rho_0=0.25\text{mm}$ 2.21   0.11 $\rho_0=1.0\text{mm}$ 0.91   0.24	$\rho_0=0.25\text{mm}$ 1.0   0.11 $\rho_0=1.0\text{mm}$ 1.4   0.12	4.55	330	42.2	135
Fe 510 pearl. red.	$\rho_0=0.25\text{mm}$ 1.55   0.53 $\rho_0=1.0\text{mm}$ 1.16   0.55	$\rho_0=0.25\text{mm}$ 0.88   0.48 $\rho_0=1.0\text{mm}$ 1.55   0.46	50	383	110.3	284

Table 1 - tensile tests, quantitative metallographic results and calculated  $l_c$

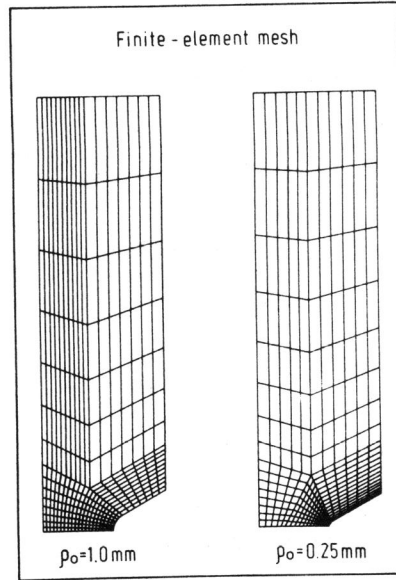


Figure 1 finite element mesh

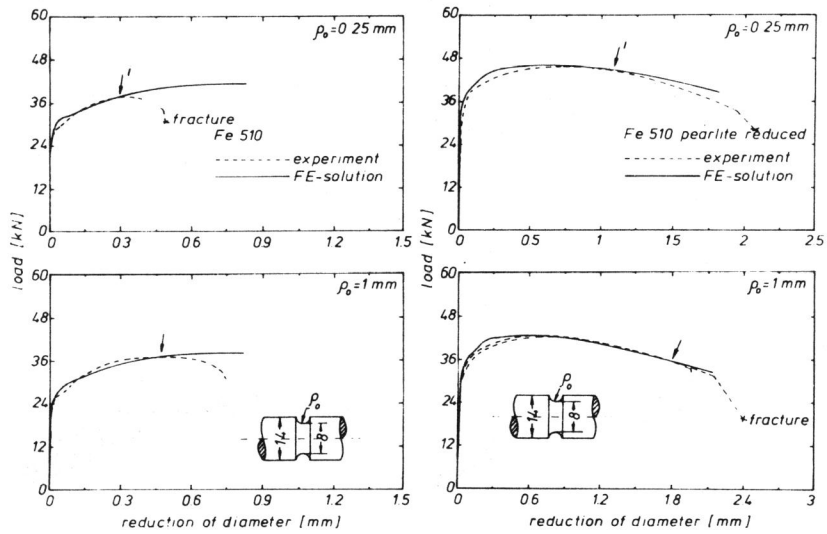


Figure 2 tensile tests, experiments and calculated

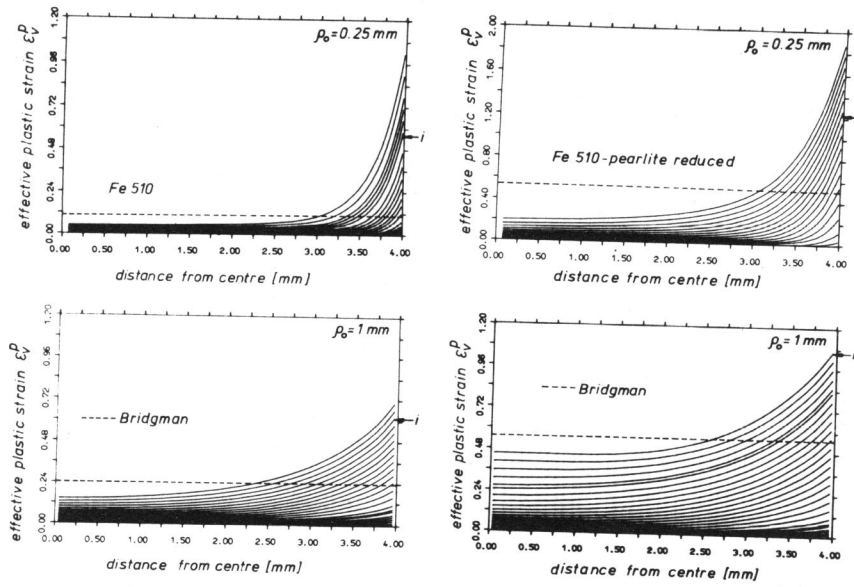


Figure 3 effective plastic strain, calculated

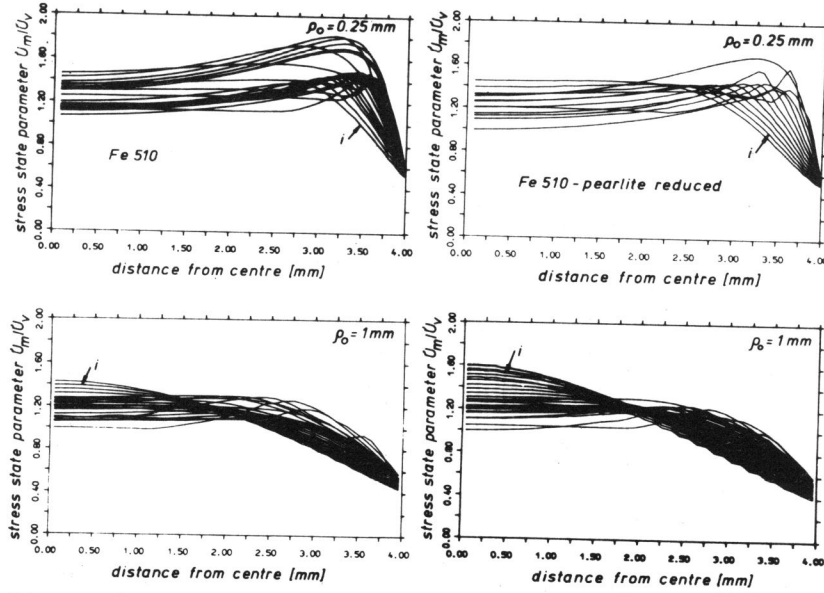


Figure 4 stress state parameters, calculated



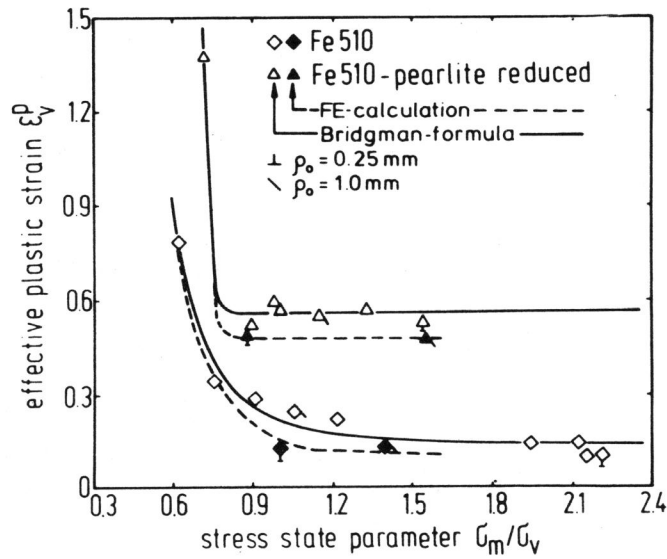
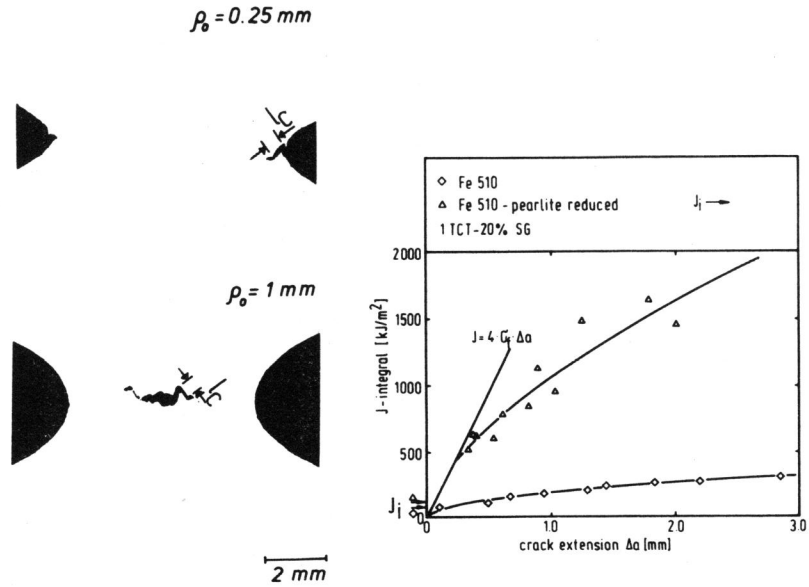


Figure 6 effective plastic strain vs. stress state